DMK | Deutschschweizerische Mathematikkommission des VSMP
(Verein Schweizerischer Mathematik- und Physiklehrkräfte)

Stochastics

Theory and Exercises for 'Sekundarstufe II'

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