Chapman & Hall/CRC Interdisciplinary Statistics Series

Age-Period-Cohort Analysis

New Models, Methods, and Empirical Applications

Yang Yang and Kenneth C. Land



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