

Chemical Theory beyond the Born-Oppenheimer Paradigm

Nonadiabatic Electronic and Nuclear Dynamics
in Chemical Reactions

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