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Physics of Solar Cells

From Basic Principles to Advanced Concepts

2nd, updated and expanded edition

Problems and Solutions by Uli Würfel



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