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Vapor-Liquid Interfaces, Bubbles and Droplets

Fundamentals and Applications

With 74 Figures



Springer

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